

Q. A 588 cm^3 vol of moist sand weighs 1010 gm , its dry unit weights is 918 gm and specific gravity of solid G_s is 2.67 . assuming the density of water as 1 gm/cc the void ratio is ?

given, volume $v = 588 \text{ cm}^3$ (cgs system)

$$\text{total weight } W = 1010 \text{ gm}$$

$$\text{dry weight } W_d = 918 \text{ gm}$$

$$G_s = 2.67$$

$$\gamma_w = 1 \text{ gm/cc}$$

$$e = ?$$

$$\begin{aligned} \gamma_d \text{ or } \gamma_s &= \frac{W_d}{V} \\ &= \frac{918 \text{ gm}}{588 \text{ cm}^3} \\ &= 1.56 \text{ gm/cm}^3 \end{aligned}$$

$$\text{also, } \gamma_d = \frac{G_s \gamma_w}{1+e}$$

$$1.56 \text{ gm/cc} = \frac{2.67 \times 1 \text{ gm/cc}}{1+e}$$

$$\Rightarrow 1+e = \frac{2.67}{1.56}$$

$$\Rightarrow e = \frac{2.67}{1.56} - 1 = 0.71$$

$$e = 0.71 \text{ ans.}$$

Density Index (I_D)

- also known as relative density or degree of density.
- used to express relative compactness of a natural soil deposit.

$$I_D = \frac{e_{\max} - e_{\text{natural}}}{e_{\max} - e_{\min}}$$

e_{\max} = void ratio in the loosest state

e_{\min} = void ratio in the densest state

e_{natural} = natural void ratio of the deposit.

- used for cohesionless soil only.
- (a) loosest form $e_{\text{natural}} = e_{\max}$, $I_D = 0$
- (b) Densest form $e_{\text{natural}} = e_{\min}$, $I_D = 1$

So, $0 < I_D < 1$ For intermediate state

or $0 < I_D < 100\%$ if expressed in Percentage.

cohesionless

Q A given soil mass has $e_{\max} = 0.85$ and $e_{\min} = 0.5$. In the field the soil is compacted to a mass density of 1800 kg/m^3 at a water content of 8% . Take the mass density of water as 1000 kg/m^3 and $G = 2.7$. The relative density of soil is?

given ; $e_{\max} = 0.85$ (loosest state)

$e_{\min} = 0.5$ (densest state)

$w = 8\%$

$G = 2.7$

$\gamma = 1800 \text{ kg/m}^3$, $\gamma_w = 1000 \text{ kg/m}^3$

$$I_D = \frac{e_{max} - e_{natural}}{e_{max} - e_{min}} \times 100$$

$$\gamma = \frac{(G + S) \gamma_w}{1 + e}$$

$$S_e = q_w = 2.7 \times 8\%$$

$$= 2.7 \times \frac{8}{100}$$

$$= 2.7 \times 0.08$$

$$= 0.216$$

$$1800 \text{ kg/m}^3 = \frac{(2.7 + 0.216) \times 1000 \text{ kg/m}^3}{1 + e}$$

$$1 + e = \frac{(2.7 + 0.216) \times 1000}{1800}$$

$$e = 1.62 - 1$$

$$e = 0.62 \quad e_{natural}$$

$$I_D = \frac{e_{max} - e_{natural}}{e_{max} - e_{min}} \times 100$$

$$= \frac{0.85 - 0.62}{0.85 - 0.5} \times 100$$

$$= 65.7\% \quad \text{ans}$$

Q A partially saturated sample from a borrow pit has a natural moisture content of 15% and bulk unit of 1.9 g/cc. The specific gravity of solids is 2.70. Determine the degree of saturation, void ratio and saturated unit weight.

given data -

$$w = 15\% = 0.15$$

$$\gamma_b \text{ or } \gamma_t \text{ or } \gamma = 1.9 \text{ gm/cc}$$

$$G_s = 2.70$$

$$s, e, \gamma_{sat} = ?$$

$$\checkmark \quad \gamma = \frac{(G_s + se) \gamma_w}{1 + e}$$

$$\gamma_d = \frac{\gamma}{1 + w}$$

$$\gamma_d = \frac{1.9 \text{ gm/cc}}{1 + 0.15} = \frac{1.9}{1.15} = 1.65 \text{ gm/cc}$$

again $\gamma_d = \frac{G_s \gamma_w}{1 + e}$

$$1 + e = \frac{G_s \gamma_w}{\gamma_d}$$

$$e = \frac{G_s \gamma_w}{\gamma_d} - 1$$

$$= \frac{2.7 \times 1}{1.65} - 1$$

$$= 1.63 - 1$$

$$e = 0.63 \quad \text{ans}$$

$$se = qw$$

$$s = \frac{qw}{e} = \frac{2.7 \times 0.15}{0.63} = 0.64 \text{ or } 64\%$$

$$\gamma_{sat} = \frac{(G + se) \gamma_w}{1 + e} ; s = 1$$

$$= \frac{(G + e) \gamma_w}{1 + e}$$

$$= \frac{(2.7 + 0.65) \times 1}{1 + 0.65}$$

$$= 2.04 \text{ gm/cc}$$